

	Pre-Kindergarten	Kindergarten	Grade 1	Grade 2	Grade 3	Grade 4	Grade 5		
20 days	M1: Numbers to 5 (45 days)	M1: Numbers to 10 (43 days)	M1: Sums and Differences to 10 (45 days)	M1: Sums and Differences to 20 (10 days)	M1: Properties of Multiplication and Division and Solving Problems with Units of 2-5 and 10 (25 days)	M1: Place Value, Rounding, and Algorithms for Addition and Subtraction (25 days)	M1: Place Value and Decmal Fractions (20 days)	20 days	
				M2: Addition and Subtraction of Length Units (12 days)					
20 days				M3: Place Value, Counting, and Comparison of Numbers to 1000 (25 days)	M2: Place Value and Problem Solving with Units of Measure (25 days)	*M2: Unit Conversions (7 days)	M2: Multi-Digit Whole Number and Decmal Fraction Operations (35 days)	20 days	
20 days	M2: Two-Dimensional and Three-Dimensional Shapes (15 days)	*M2: 2D and 3D Shapes (12 days)				M3: Multi-Digit Multiplication and Division (43 days)			20 days
20 days	M3: Counting to Answer Questions of How Many (50 days)	M3: Comparison of Length, Weight, Capacity, and Numbers to 10 (38 days)	M2: Introduction to Place Value Through Addition and Subtraction Within 20 (35 days)	M4: Addition and Subtraction Within 200 with Word Problems to 100 (35 days)	M3: Multiplication and Division with Units of 0, 1, 6-9, and Multiples of 10 (25 days)			M3: Addition and Subtraction of Fractions (22 days)	20 days
20 days				M3: Ordering and Comparing Length Measurements as Numbers (15 days)	M5: Addition and Subtraction Within 1000 with Word Problems to 100 (24 days)	M4: Multiplication and Area (20 days)	M4: Angle Measure and Plane Figures (20 days)	M4: Multiplication and Division of Fractions and Decmal Fractions (38 days)	20 days
20 days			M4: Number Pairs, Addition and Subtraction to 10 (47 days)	M4: Place Value, Comparison, Addition and Subtraction to 40 (35 days)	M5: Foundations of Multiplication and Division (24 days)	M5: Fractions as Numbers on the Number Line (35 days)	M5: Fraction Equivalence, Ordering, and Operations (45 days)		
20 days		M4: Comparison of Length, Weight, and Capacity (35 days)			M5: Identifying, Composing, and Partitioning Shapes (15 days)				M6: Collecting and Displaying Data (10 days)
20 days	M5: Numerals to 5, Addition and Subtraction Stories, Counting to 20 (35 days)	M5: Numbers 10-20 and Counting to 100 (30 days)	M6: Place Value, Comparison, Addition and Subtraction to 100 (35 days)	M7: Problem Solving with Length, Money, and Data (30 days)	M7: Geometry and Measurement Word Problems (40 days)	M6: Decimal Fractions (20 days)	M6: Problem Solving with the Coordinate Plane (40 days)	20 days	
20 days								M8: Time, Shapes, and Fractions as Equal Parts of Shapes (20 days)	

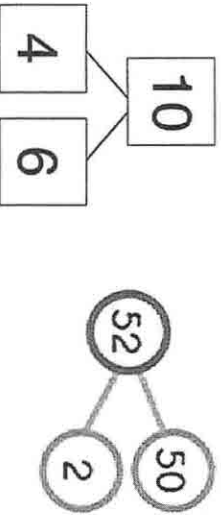
Approx. test date for grades 3-5

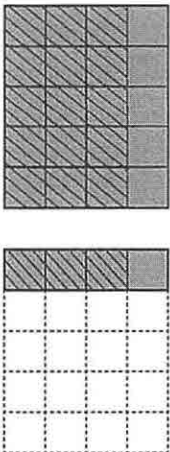
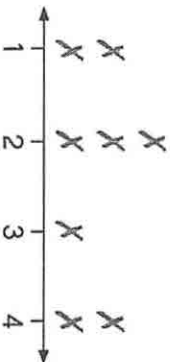
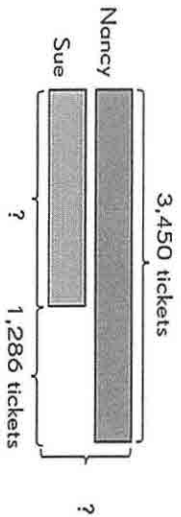
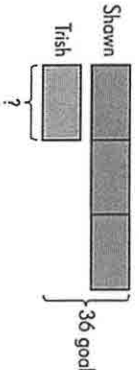
*Please refer to grade-level descriptions to identify partially labeled modules and the standards corresponding to all modules.


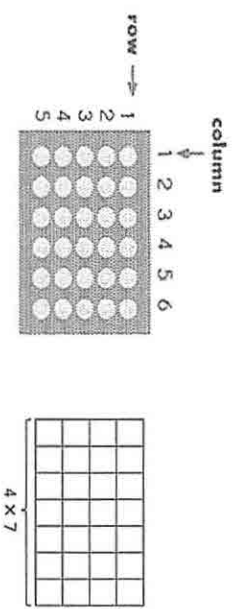
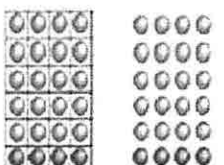
Key:	Geometry	Number	Number and Geometry, Measurement	Fractions
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Key Fluencies

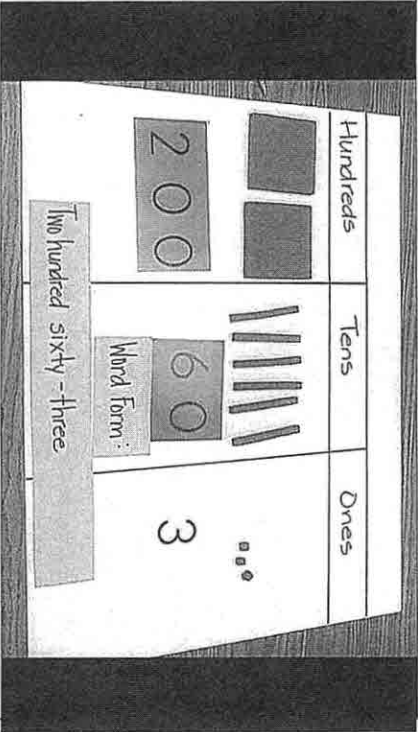
Grade	Required Fluency
K	Add/subtract within 5
1	Add/subtract within 10
2	Add/subtract within 20 Add/subtract within 100 (pencil and paper)
3	Multiply/divide within 100 Add/subtract within 1000
4	Add/subtract within 1,000,000
5	Multi-digit multiplication
6	Multi-digit division Multi-digit decimal operations
7	Solve $px + q = r$, $p(x + q) = r$
8	Solve simple 2×2 systems by inspection

Term	Description	Visual Representation
Number Bond	A representation that helps students see that whole numbers and fractions can be decomposed (broken up) into parts. Students can see the relationships between numbers through this model.	 <p>Diagram illustrating Number Bonds: 10 is composed of 4 and 6; 52 is composed of 50 and 2.</p>
Addition Vocabulary		<p>Addition:</p> $\begin{array}{r} 8 + 3 = 11 \\ \text{Addend} \quad \text{Addend} \quad \text{Sum} \end{array}$
Subtraction Vocabulary		$\begin{array}{r} 18 - 11 = 7 \\ \text{minuend} \quad \text{subtrahend} \quad \text{difference} \end{array}$
Multiplication Vocabulary		<p>Multiplication:</p> $\begin{array}{r} 6 \times 3 = 18 \\ \text{Factor} \quad \text{Factor} \quad \text{Product} \end{array}$ <p>(or Multiplier) (or Multiplicand)</p>
Division Vocabulary		<p>Division</p> $\begin{array}{r} 7 \div 2 = 3 \text{ rem. } 1 \\ \text{Dividend} \quad \text{Quotient} \quad \text{Remainder} \end{array}$ <p>Divisor</p>
Fraction Vocabulary		$\frac{3}{5}$ <p>← numerator ← denominator</p> <p>$\frac{7}{5} \rightarrow 1\frac{2}{5}$ Improper Fraction → Mixed Number</p>
Equation	The statement that two expressions are equal. Must have an = symbol.	$5 + 9 = 45$ $12 \times 6 = 72$
Expression	A number or a group of numbers with operation symbols, no = symbol.	$5 + 9$ 12×6

Partial Products	Similar to the area model, it breaks each number into the value of the digits and each value is multiplied with the other values.	$\begin{array}{r} 67 = 60 + 7 \\ \times 45 \\ \hline 40 \times 60 = 2400 \\ 40 \times 7 = 280 \\ 5 \times 60 = 300 \\ 5 \times 7 = 35 \\ \hline 3,015 \end{array}$
Area Model for Fractions	A way to pictorially represent fractions and operations with fractions.	$\frac{6}{5} \times \frac{3}{4} = \frac{3}{4} \times \frac{6}{5}$ $\frac{18}{20} = \frac{9}{10}$ 
Line Plot	A representation of data (like a graph) using a number line and x's to represent the data.	
Tape Diagram/Bar Model	Pictorial representation of relationships between quantities used to solve word problems.	<p>Nancy and Sue sold tickets for a concert. Nancy sold 3,450 tickets. Sue sold 1,286 fewer tickets than Nancy.</p>  <p>Shawn and Trish scored 36 goals in all. Shawn scored 3 times as many goals as Trish. How many goals did Trish score?</p> <p>4 units \longrightarrow 36 1 unit \longrightarrow 36 \div 4 = 9</p> 

Equal Groups	In multiplication, each group has the same amount in the group. This is a visual representation for multiplication.	 $4 \text{ groups of } 2 = 8$ $4 \times 2 = 8$												
Array	Objects organized into equal rows (going across) and columns (going down). Used as a model for multiplication.	 <div style="border: 1px solid black; padding: 5px; margin: 10px 0;">$5 \times 6 = ?$ $5 \text{ rows of } 6 = 30$</div>												
Distributive Property	The property of numbers that relates addition to multiplication. The product of a number and a sum is equal to the sum of the products of the number and the two addends.	<div style="display: flex; align-items: center;"><div style="border: 1px solid black; padding: 10px; margin-left: 20px;">$4 \times 6 =$ $4 \times 5 = 20 \div 4 \times 1 = 4$ $20 + 4 = 24$</div></div> $4 \times 6 = 4 (5 + 1) = 4 \times 5 + 4 \times 1$												
Area Model for Multiplication	Similar to the array. Strategy used for multiplying based on place value. The digits are broken up into their values and multiplied.	<div style="display: flex; align-items: center; justify-content: center;"><div style="text-align: center;">$60 + 7$<table style="border-collapse: collapse;"><tr><td style="padding: 5px;">40</td><td style="padding: 5px;">2400</td><td style="padding: 5px;">280</td></tr><tr><td style="padding: 5px;">5</td><td style="padding: 5px;">300</td><td style="padding: 5px;">35</td></tr></table></div><div style="margin: 0 20px;">+</div><div style="text-align: center;"><table style="border-collapse: collapse;"><tr><td style="padding: 5px;">2400</td><td style="padding: 5px;">280</td></tr><tr><td style="padding: 5px;">300</td><td style="padding: 5px;">35</td></tr><tr><td colspan="2" style="border-top: 1px solid black; padding-top: 5px;">$3,015$</td></tr></table></div></div> $67 \times 45 =$	40	2400	280	5	300	35	2400	280	300	35	$3,015$	
40	2400	280												
5	300	35												
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300	35													
$3,015$														

Renaming/ Regrouping	Changing the unit while keeping the value of a number the same. This is an important concept to understand as students then work with operations and need to rename/regroup numbers (you may have called this borrowing and carrying when working with an operation).	Number Form	Unit Form	Renaming
		15	1 ten five ones	15 ones
		37	3 tens 7 ones	37 ones or... 2 tens 17 ones
		124	1 hundred two tens 4 ones	12 tens 4 ones ...
Decompose	Breaking a number down into smaller parts. Students can use number bonds and/or place value knowledge to work with parts.	$\begin{array}{r} & 1 & & 1 \\ 3 & 4, & 5 & 2 & 8 \\ + & 4 & 2, & 9 & 6 & 5 \\ \hline & 4 & 9 & 3 \end{array}$ <p>5 hundreds + 9 hundreds = 14 hundreds = 1 thousand 4 hundreds</p>		
Partial Sums	A way to add multi-digit numbers by decomposing the numbers and adding the parts.	$\frac{10}{12} = \frac{5}{12} + \frac{5}{12} \quad \text{or} \quad \frac{2}{12} + \frac{3}{12} + \frac{1}{12} + \frac{4}{12}$ $\begin{array}{c} 25 + 14 = 39 \\ \begin{array}{c} 20 \quad 5 \\ \diagdown \quad \diagup \\ 30 \quad 10 \\ \diagup \quad \diagdown \\ 30 + 9 = 39 \end{array} \end{array}$ $\begin{array}{r} 268 \\ + 483 \\ \hline 600 \\ \text{Add 100s} \\ 140 \\ \text{Add 10s} \\ + 11 \\ \text{Add 1s} \\ \hline 751 \\ \text{Add partial sums.} \end{array}$ $\begin{array}{c} 24 \quad + \quad 33 \\ \diagdown \quad \diagup \quad \diagdown \quad \diagup \\ 20 \quad 4 \quad 30 \quad 3 \\ (20 + 30) + (4 + 3) = 57 \end{array}$		
Partial Differences	A way to subtract multi-digit numbers by decomposing a number and subtracting the parts.	$34 - 17 = 34 - 10 = 24$ $24 - 7 = 17$ <p>Break up the 17 into 10 and 7. Begin with the 34 and subtract the 10 and then the 7.</p>		

Place Value Chart	A chart to organize numbers or manipulatives into their place based on the value of the digits.													
		Base Ten Blocks on a Place Value Chart												
Standard Form		Place Value Chips on a Place Value Chart												
Word Form		Standard form: 2,478												
Expanded Form		The word form of 2,475 is two thousand, four hundred seventy-five.												
Unit Form	Breaking a number into place value units.	$2,000 + 400 + 70 + 5$ is the expanded form of 2,475. <table><tr><th>Number Form (Standard Form)</th><th>Expanded Form</th><th>Unit Form</th></tr><tr><td>15</td><td>$10+5$</td><td>1 ten five ones</td></tr><tr><td>235</td><td>$200+30+5$</td><td>2 hundreds 3 tens 5 ones</td></tr><tr><td>110</td><td>$100+10$</td><td>1 hundred 1 ten</td></tr></table>	Number Form (Standard Form)	Expanded Form	Unit Form	15	$10+5$	1 ten five ones	235	$200+30+5$	2 hundreds 3 tens 5 ones	110	$100+10$	1 hundred 1 ten
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